

Summary of Post-quantum Signature Schemes

Approach	Instantiation	Remarks
<b>Without trapdoors</b>		
<b>Hash-based</b> OWF $\rightarrow$ OTS $\xrightarrow{*}$ Sign *: Merkle tree [Mer90]	SHA family [BDH11] and many variants, stateless scheme [BHH <sup>+</sup> 15]	Need: more quantum cryptanalysis considering internal design of SHA
<b>“Homomorphic” hash</b> hash $\rightarrow$ ID $\xrightarrow{*}$ Sign *: Fiat-Shamir	<b>Lattice:</b> safety check with aborting. SIS [Lyu08, KTX08], Ring-SIS [Lyu09], both [Lyu12, DDLL13] <b>Code:</b> [Ste96] <b>MQ:</b> N/A	[KTX08] inspired by [Ste96]. Adapt ideas from lattice ID to code-based? Quantum security unclear: quantum rewinding+FS in QRO
<b>With trapdoors</b>		
<b>“Text-book” RSA</b> $\sigma = f^{-1}(sk, m)$ e.g. $\sigma = m^d \pmod{N}$	<b>Lattice:</b> [GGH97], NTUSign [HPS01, HHGP <sup>+</sup> 03] (broken [NR09, DN12]) <b>Code:</b> early proposals broken <b>MQ:</b> majority (many broken)	Bad idea, <b>avoid!</b>
<b>Hash-&amp; Sign in RO (Full-domain hash)</b> $\sigma = f^{-1}(sk, \mathcal{O}(m))$ $\mathcal{O}$ : random-oracle	<b>Lattice:</b> [GPV08, MP12] <b>Code:</b> [CFS01]. Formal proof of CFS01 in [Dal07], but one of the assumptions was disproved in [FGUO <sup>+</sup> 13].	adapt lattice ideas to code? Fix [CFS01] proof?
Direct constructions <b>without RO</b>	<b>Lattice:</b> [Boy10, CHKP12, DM14, AS15]	provably secure code & MQ-based unclear

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